## **Quadratic Equations**



## **Chapter Review**



### Solving by Taking Square Roots

- · Always two solutions in quadratic equations
- · Can not take the square-root of a negative number - in the Real Number system

Example, 
$$\sqrt{9}$$
  $\sqrt{-9}$  — Not a Real Number - the Answer is a Complex number

Steps

- 1. Isolate the "x2" term
- 2. Take the square-root of both sides

Example 
$$2x^{2}-4=10$$

$$+4+4$$

$$2x^{2}=14$$

$$x^{2}=7$$
Step 2 
$$\sqrt{x^{2}}=\sqrt{7}$$

$$x=\sqrt{7}$$

$$x=\sqrt{7}$$

$$x=\sqrt{7}$$

## **Graphing Quadratic Equations**

Steps

1. Find the vertex

("u"-shape)

2. Graph - the shape is always a parabola

Example 
$$y = 2x^2 + 4x - 8$$

Finding vertex - write equation is standard form (highest -> lowest power, ax2+bx+C=0)

Find 
$$-\frac{b}{2a} = \frac{-(4)}{2(2)} = \frac{-4}{4} = -1$$

Find  $f(-\frac{b}{2a}) \rightarrow \text{plug in } -\frac{b}{2a}$  into equation

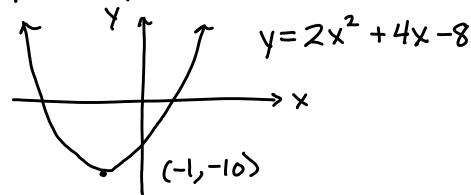
$$y=2x^{2}+4x-8$$

$$=2(-1)^{2}+4(-1)-8=2(1)+-4-8=-10$$

Vertex 
$$(-1,-10)$$
,  $y=2x^2+4x-8$ 

$$y = 2x^2 + 4x - 8$$

X2 term is positive graph upward parabola X term negative - downward Graph upward parabola from (-1,-10)





## Quadratic Formula

· Very important! Need to master it to solve quadratic equations

When you have  $ax^2 + bx + c = 0$ 

the solutions are

$$x = -b \pm \sqrt{b^2 - 4ac}$$
2a

plug in values ¿ into formula

$$X = -(-9)^{2}\sqrt{(-9)^{2}-4(1)(8)}$$

$$Z(1)$$

$$X = \frac{9 \pm \sqrt{81 - 32}}{2}$$

$$x = \frac{9 \pm \sqrt{49}}{2}$$

Example solve

$$\chi^{2} - 9\chi = -8$$

First write in Standard form  $1x^2-9x+8=0$  $1x^2-9x+8=0$ 

$$X = 9 + 7$$
  $X = 9 - 7$   $Z$ 

$$solutions \rightarrow X = 8$$



# Solve Quadratic Equations by Factoring

- · Need to know how to factor polynomials
- · Only works when you can factor otherwise use quadratic formula
- · Based on zero-product property

Example 
$$x^2-9x+8=0$$
 Factor first  $(x-1)(x-8)=0$ 

Zero One of these terms must be zero, because that's the only way you can product the equation (left side) can be equal to Zero (right side)

Solve by setting both factors equal to zero

$$X-1=0$$

$$\frac{X-1=0}{X=8} \leftarrow \text{Solutions}$$



# ▼ The Discriminant- Type of Roots

$$X = -b \pm \sqrt{b^2 - 4ac}$$
 $\leftarrow$  the  $b^2 - 4ac$  part is the Discriminant

When:

$$b^2$$
- $4ac=0$   $b^2$ - $4ac=positive$   $b^2$ - $4ac=negative$ 

I double root 2 real roots No real roots

Note: "root" - means solutions

## Completing the Square

· A method to rewrite a quadratic equation in such a way as to solve by taking the square-root of both sides

move c to  $\chi^2 - 9\chi + 8 = 0$  right side Example x<sup>2</sup>-9x 1. write in  $x^2 - 9x + (-\frac{9}{2})^2 = -8 + (-\frac{9}{2})^2$ Standard form (ax2+bx+c=0)  $= \frac{x^2 - 9x + 81}{4} = -8 + 81$ add (b) to  $(x-\frac{9}{2})^2 = \frac{49}{4}$ Factor both sides solve by taking V both sides X - 9 = ± ½ X - 9 = 7 X- 7=-1  $x = \frac{7}{2} + \frac{9}{2} = \frac{16}{2} = 8$  $X = -\frac{7}{2} + \frac{9}{2} = \frac{2}{2} = \frac{1}{2}$ 

# **Graphing Quadratic Inequalities**

Graph using same steps as linear inequalities

